

Unsymmetrical Bending

The stress σ is given by

$$\frac{P}{A} + \frac{I_{xy} x - I_{yy} y}{I_{xy}^2 - I_{xx} I_{yy}} M_x + \frac{I_{xy} y - I_{xx} x}{I_{xy}^2 - I_{xx} I_{yy}} M_y$$

P is the axial force

A is the area of section

I_{xx} is the second moment of area about the x-axis

I_{yy} is the second moment of area about the y-axis

I_{xy} is the product moment of area

M_x is the BM about the x-axis

M_y is the BM about the y-axis

The location of the neutral axis is given by $\sigma =$

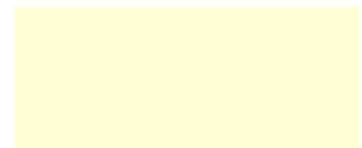
Note 1

$I_{xy} = 0$ for a rectangle

Note 2

Shift theorem

$$I_{xy} = I_{x_c y_c} + Ahk$$



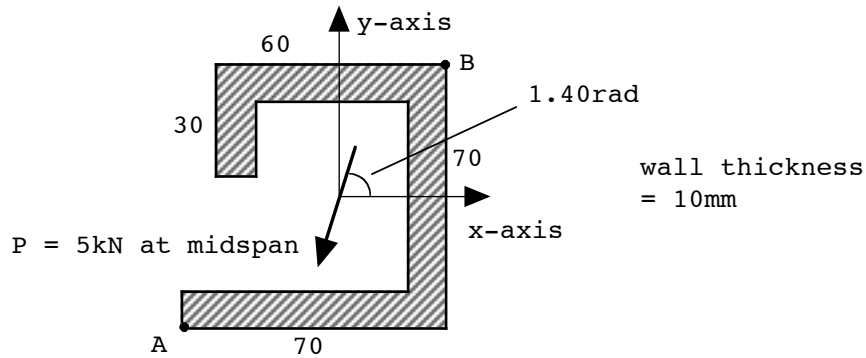
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Qu.1

A bar has the cross-section shown in Fig.1 and is used as a simple beam of length 2m. Determine the maximum tensile and compressive stresses in the beam.

$$x_C = 28\text{mm} \quad y_C = 35\text{mm} \quad I_{XX} = 1.330 \times 10^6\text{mm}^4 \quad I_{YY} = 917 \times 10^3\text{mm}^4$$

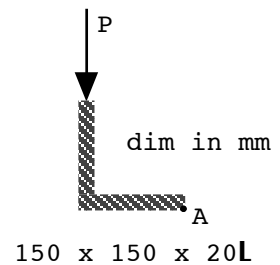
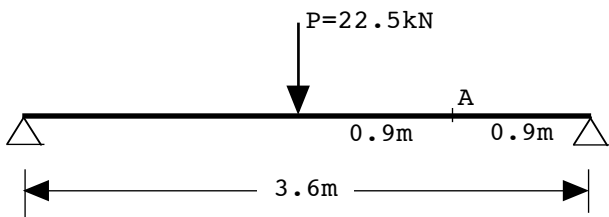
$$I_{XY} = 30 \times 10^3\text{mm}^4 \quad \alpha = 0.215\text{rad} \quad \sigma_A = 91.5\text{N/mm}^2 \quad \sigma_B = -75.8\text{N/mm}^2$$



Qu.2

In Fig.2 find the stress at point A.

$$I_{XX} = I_{YY} = 11.596 \times 10^6\text{mm}^4 \quad I_{XY} = -6.79 \times 10^6\text{mm}^4$$



Qu.3

In Fig.3 determine the largest value of M so that the allowable stress does not exceed 80N/mm^2 . All dimensions are in mm.

$$M = 266.8 \text{ N-mm}$$

